

Summarizing Low-dimensional Patterns in Long-term Echosounder Time Series from the U.S. Ocean Observatories Initiative Network

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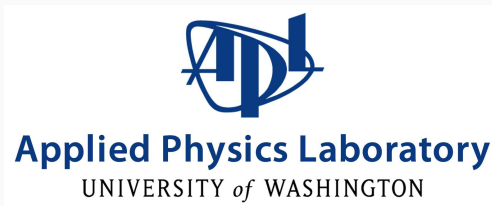
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April 25, 2022



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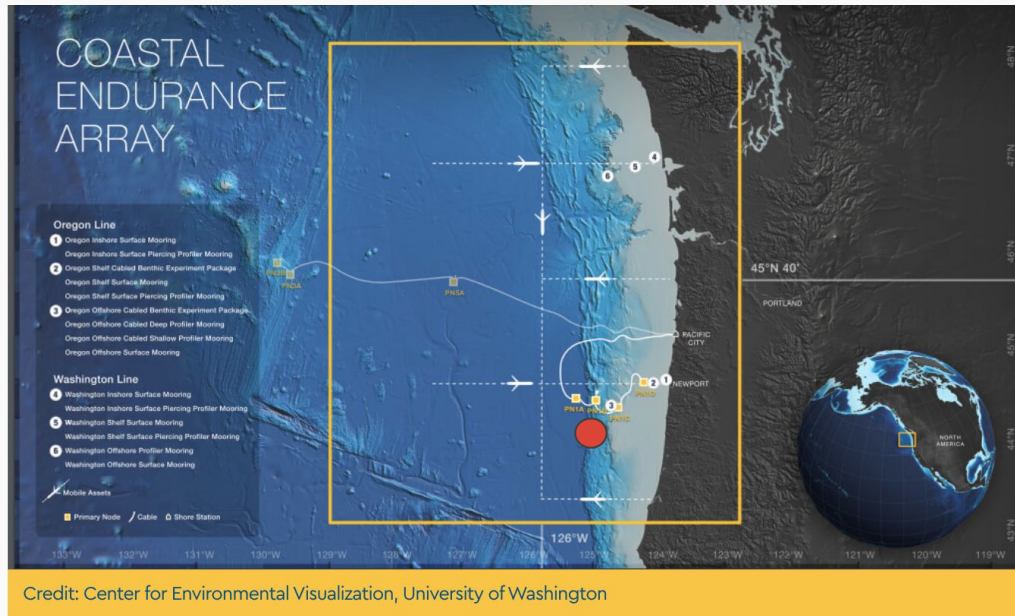


Motivation



OCEAN
OBSERVATORIES
INITIATIVE

- Continuous (24/7) moored data collection
- Commissioned since 2015
- Committed to 25+ years of operation
- Multiple instruments simultaneously sensing the environment
- Upward looking echosounders (200m)

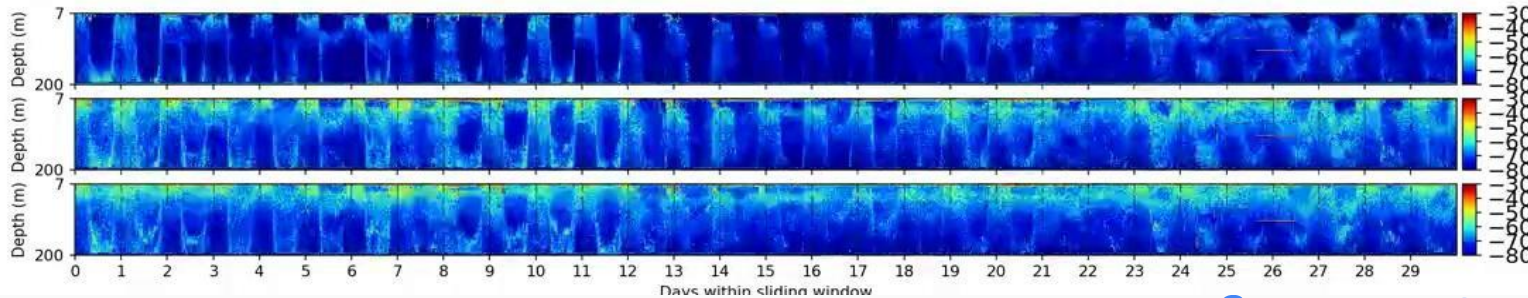


How can we extract information from these long-term time series?

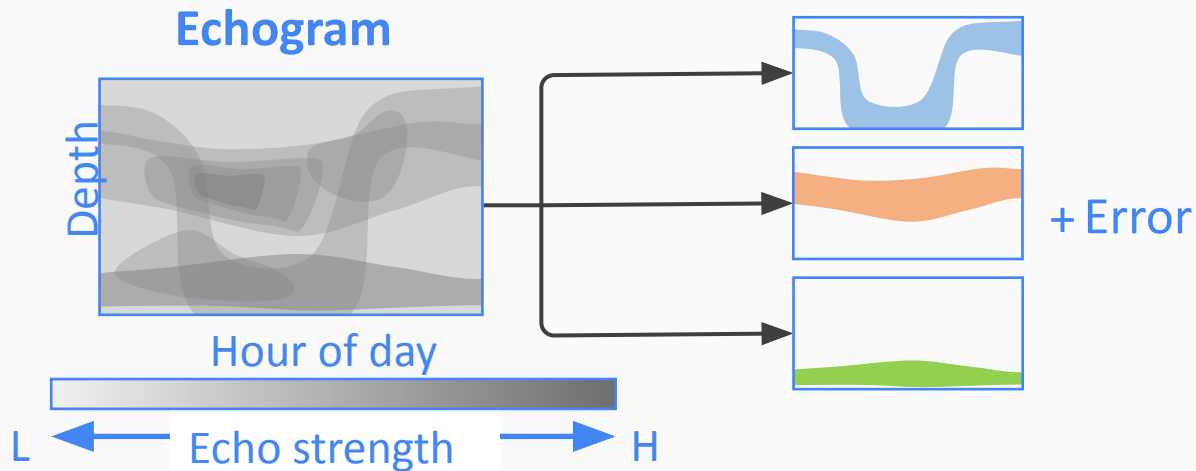
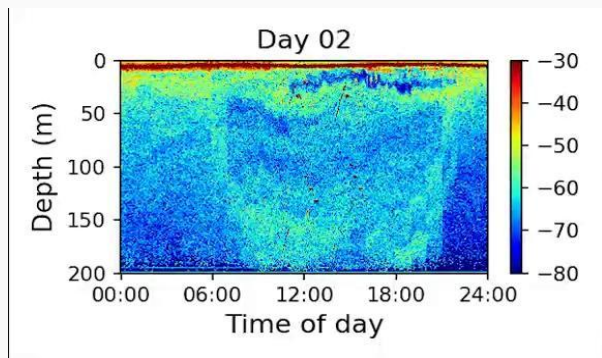
Low-dimensional Representation of Echograms

Echogram: 12 months of data

Depth (m)

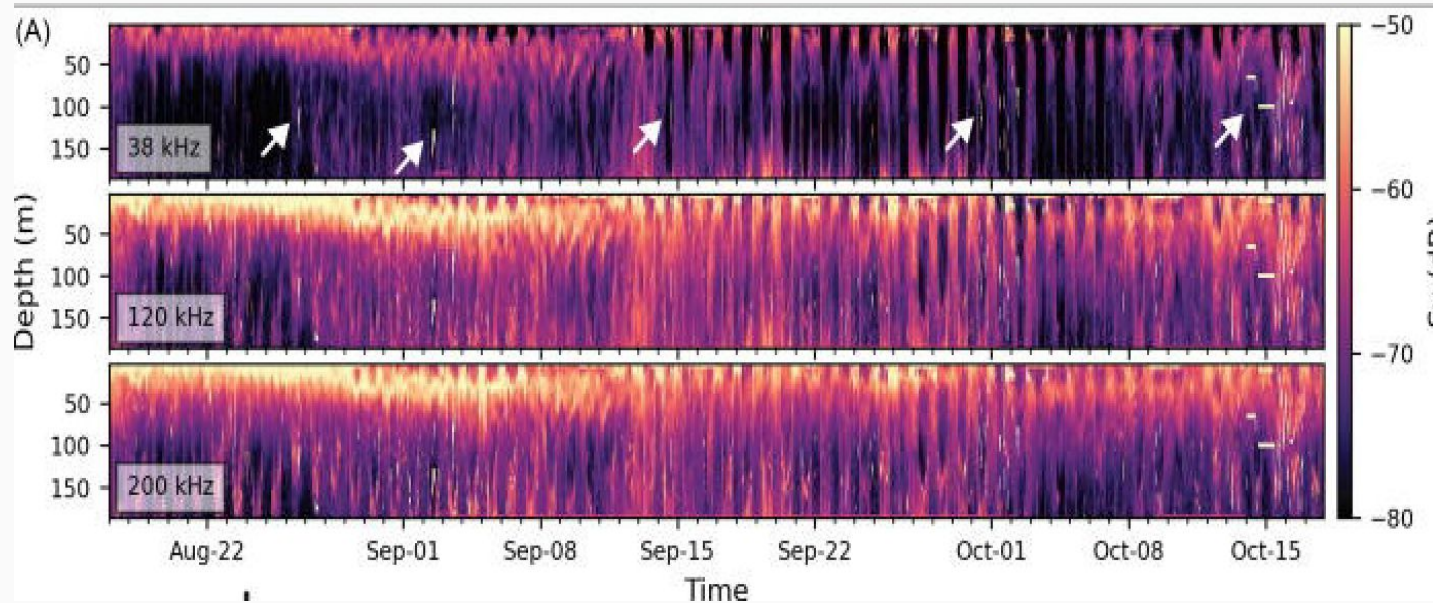


Components

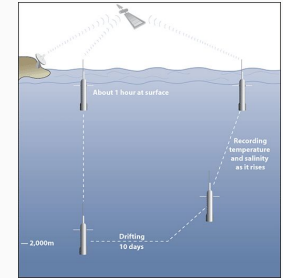


Data Outliers

2 months of data: Aug 17- Oct 17, 2015




Ocean profiler



Decomposition analysis (such as Principal Component Analysis) on data with outliers yields a corrupted result, as the magnitude of the outliers can dominate the cost.

Robust Principal Component Pursuit for Outlier Removal

$$\begin{aligned} & \min_{L,S} \|L\|_* + \gamma \|S\|_1, \\ & \text{subject to } L + S = X \end{aligned}$$


Low rank (Sonar Patterns) Sparse (Profiler Artifacts)

Rank: $\text{rank}(L) = \#$ nonzero singular values (σ_i)

Nuclear Norm: $\|L\|_* = \sum_i \sigma_i(L)$

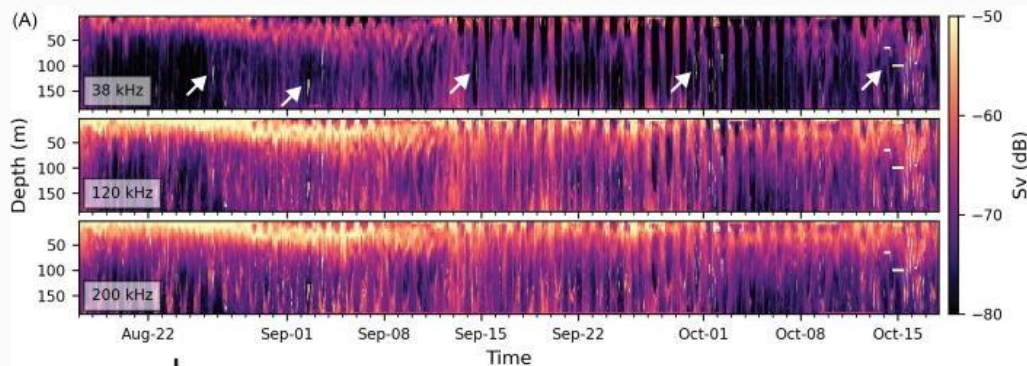
Entrywise L1-norm: $\|S\|_1 = \sum_{ij} |s_{ij}|$

*If such a decomposition exists the solution can be found **exactly**, no tuning of γ needed!*

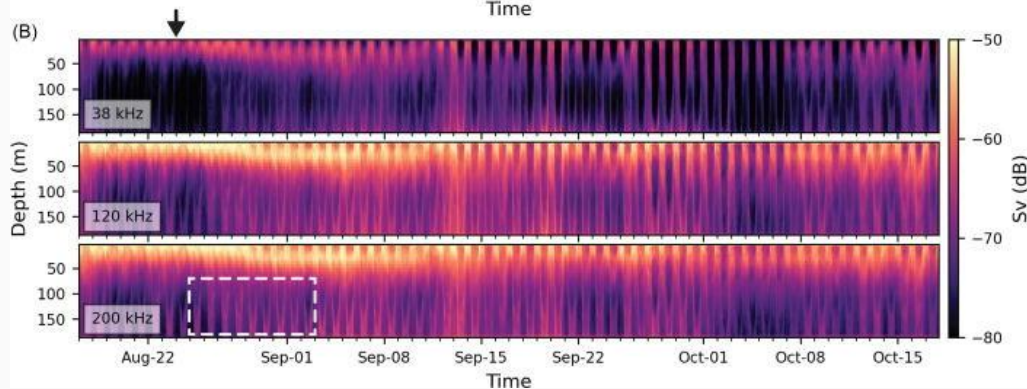
□ [Candes'09 Robust Principal Component Analysis?](#)

Robust Principal Component Pursuit for Outlier Removal

Raw Data (X)

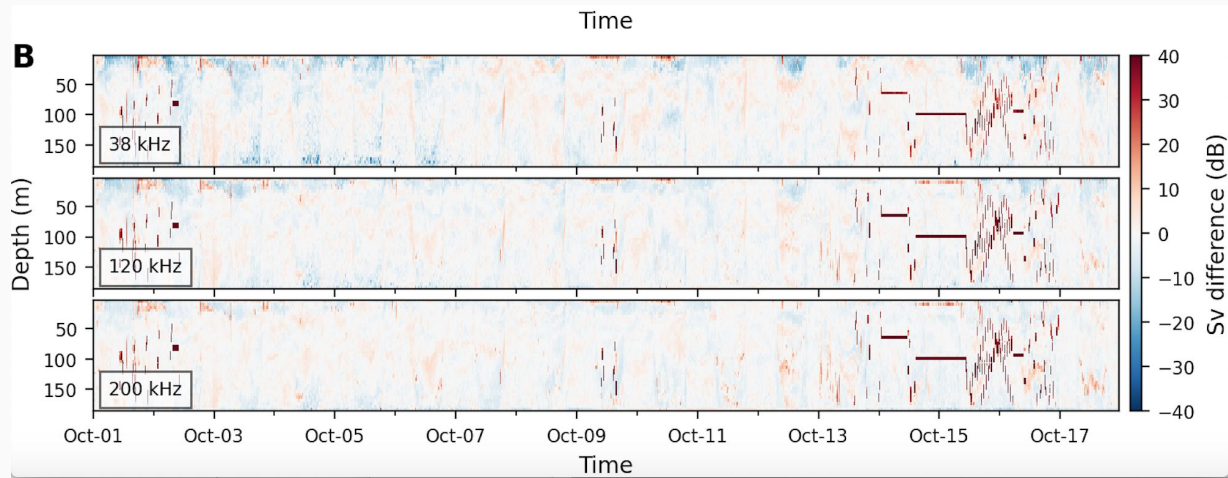


Low Rank Component (L)
Denoised Data



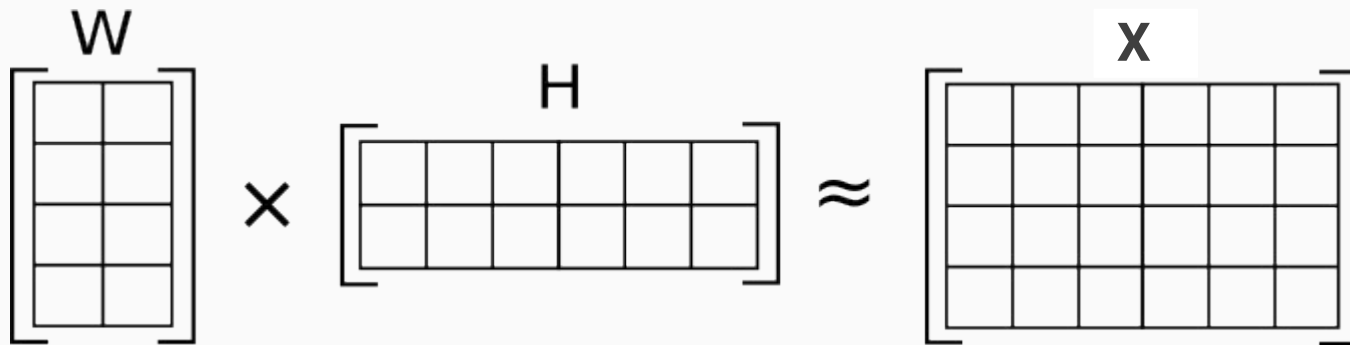
Robust Principal Component Pursuit for Outlier Removal

Sparse Component (S):



- Some signal is in the sparse component.
- There is intrinsic variation in the low rank patterns over time.
- Not crucial for extracting dominant patterns.

Nonnegative Matrix Factorization (NMF) for Echogram Pattern Discovery



Latent Variables/
Components

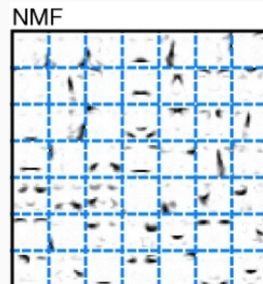
Weights/Activations

Data

$$\min_{W, H} \|X - WH\|_F^2,$$

subject to $W \geq 0, H \geq 0$

- Total backscatter is built of backscatter of individual components
- [Lee et.al., Learning the parts of objects by nonnegative matrix factorization](#)



Temporally Smooth NMF

Smooth Activations Sparseness

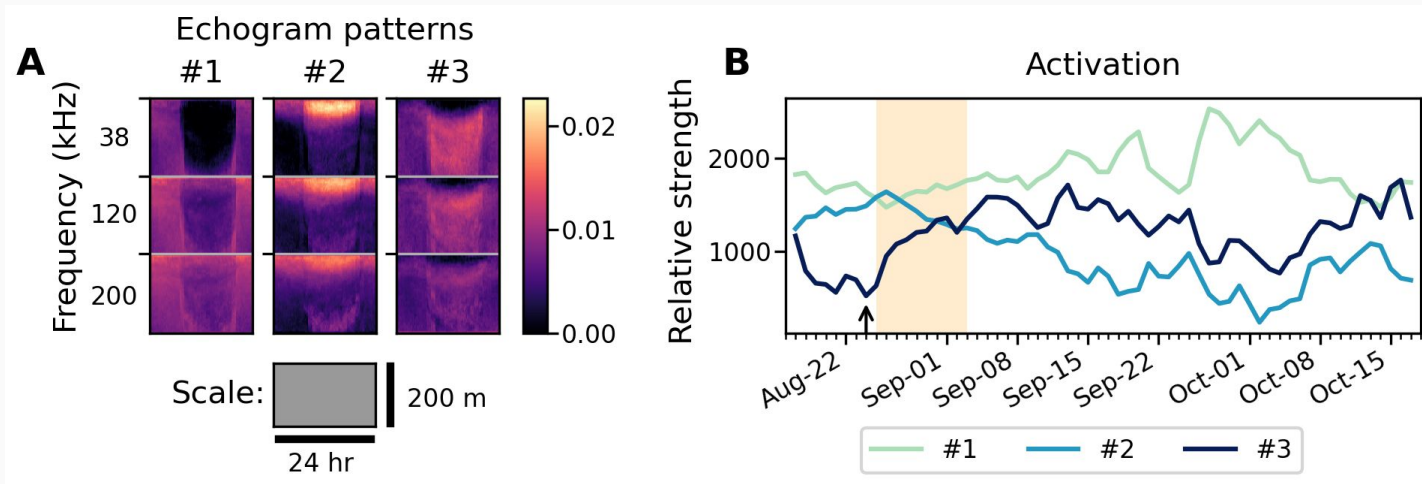


$$\min_{W, H} \|X - WH\|_F^2 + \eta \|H\Delta\|_F + \lambda \|W\|_1$$

$$\text{subject to } \mathbf{W}_{d,k} \geq 0, \mathbf{H}_{k,t} \geq 0,$$

- ❑ [Fabregat et. al., solving NMF with smoothness and sparsity constraints](#)
- ❑ Python Package: <https://pypi.org/project/time-series-nmf/>

NMF Results



- #1: DVM (zooplankton-like)
- #2: Subsurface Layer (zooplankton-like)
- #3: fish-like

In a Nutshell

- **Robust PCA** is powerful for automatically removing outliers.
- **Nonnegative Matrix Factorization** discovers biologically meaningful temporal patterns.

More details:

- Lee W.-J., Staneva V., [Compact representation of temporal processes in echosounder time series via matrix decomposition](#)

Ongoing and Future Work:

- Expand to years of Ocean Observatories Initiative data
- Analyze with conjunction with other environmental variables



THANK YOU!

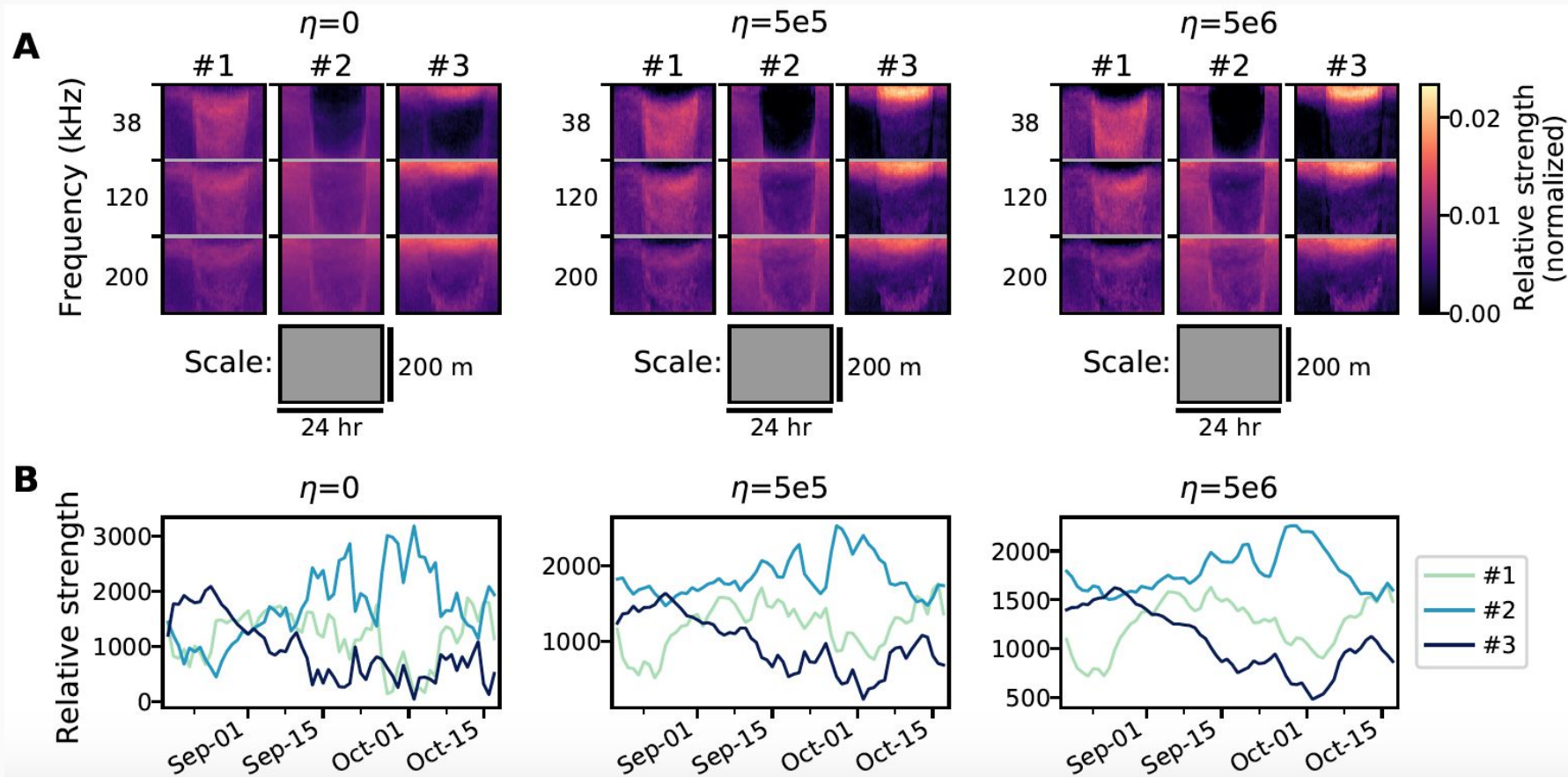


GORDON AND BETTY
MOORE
FOUNDATION



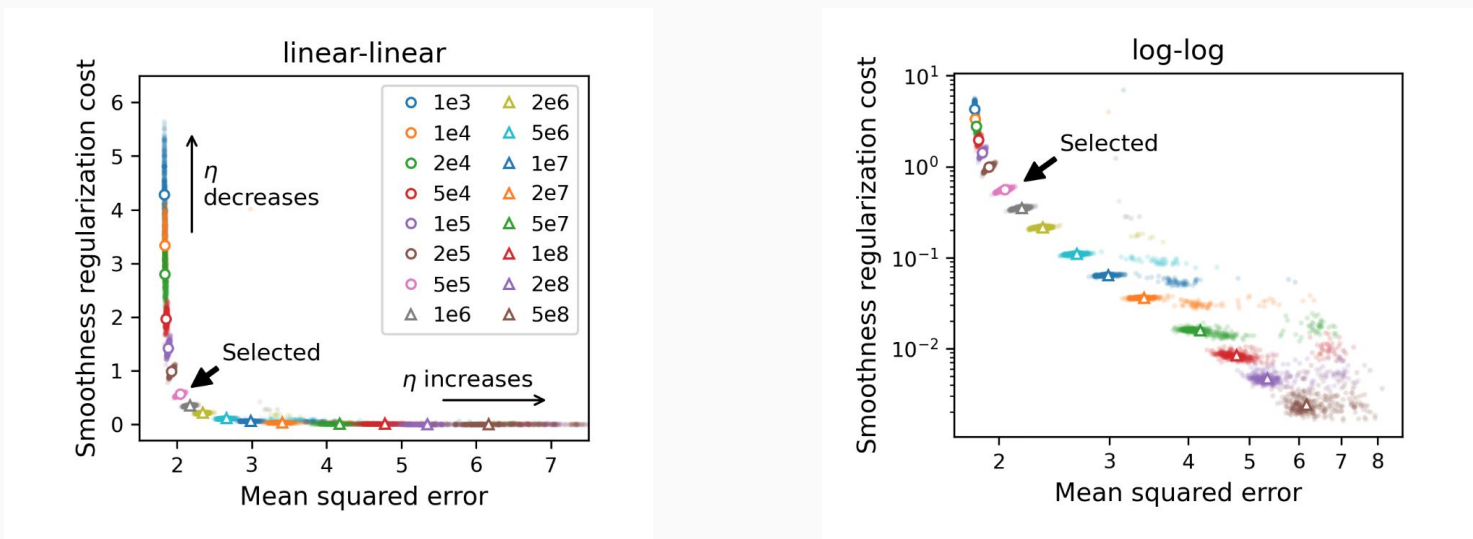
ALFRED P. SLOAN
FOUNDATION

Effect of Smoothing Parameter



L-curve Method for Selecting Regularization Parameters

Trade-off between minimization cost and smoothness.



(point cloud correspond to multiple runs)

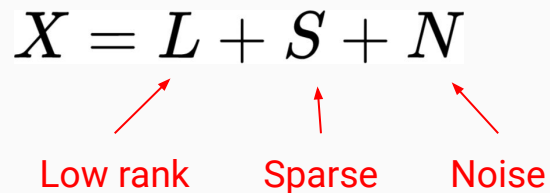
[Oraintara, S., et. al., A method for choosing the regularization parameter in generalized Tikhonov regularized linear inverse problems](#)

Robust Principal Component Pursuit for Outlier and **Noise** Removal

[\(Zhou et.al, Stable Principal Component Pursuit\)](#)

Instead Assume:

$$X = L + S + N$$


Low rank Sparse Noise

Small noise: $\|N\|_F < \delta$ we can solve the following problem

$$\begin{aligned} \min_{L,S} & \|L\|_* + \gamma \|S\|_1, \\ \text{subject to} & \|X - L - S - N\|_F < \delta \end{aligned}$$

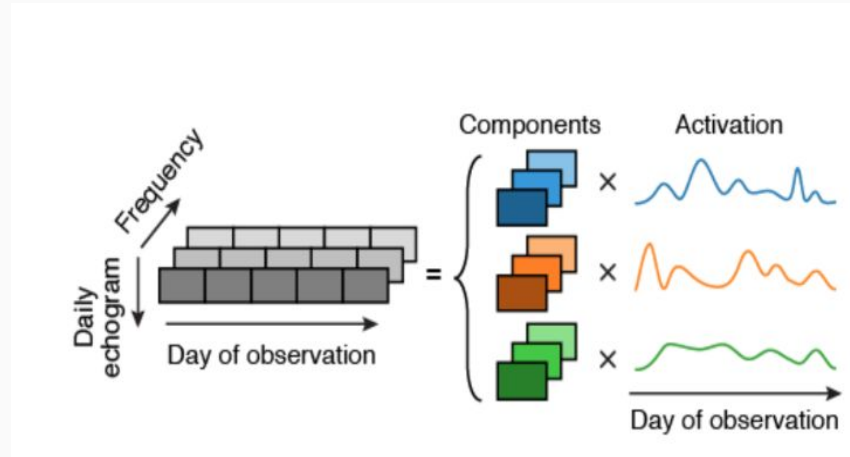
“Stable”: small noise => small reconstruction error

Extra parameter that needs to be tuned!

<https://github.com/ShunChi100/RobustPCA/>

Tensor Decomposition of Sonar Data

Treat each dimension separately?



Matrix decomposition => Tensor Decomposition

Kruskal Tensor Decomposition

2D decomposition as a sum of outer products (SVD):

$$\mathbf{X} \quad (I \times J) \quad \cong \quad \lambda_1 \begin{bmatrix} | \\ \mathbf{a}_1 \\ | \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{b}_1 \\ \text{---} \end{bmatrix} + \dots + \lambda_R \begin{bmatrix} | \\ \mathbf{a}_R \\ | \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{b}_R \\ \text{---} \end{bmatrix} = \begin{bmatrix} | & & | \\ \mathbf{A} & & \\ | & & | \end{bmatrix} \begin{bmatrix} \diagdown \\ \mathbf{D} \\ \diagup \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{B}^T \\ \text{---} \end{bmatrix}$$

$(I \times R)$ $(R \times R)$ $(R \times J)$

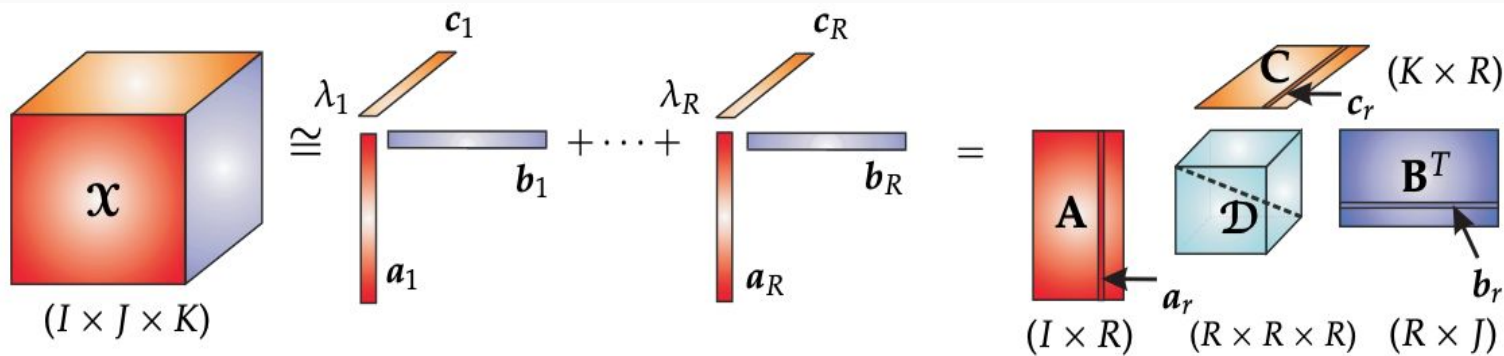
3D decomposition as a sum of outer products (higher order SVD)

$$\mathbf{x} \quad (I \times J \times K) \quad \cong \quad \lambda_1 \begin{bmatrix} | \\ \mathbf{a}_1 \\ | \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{b}_1 \\ \text{---} \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{c}_1 \\ \text{---} \end{bmatrix} + \dots + \lambda_R \begin{bmatrix} | \\ \mathbf{a}_R \\ | \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{b}_R \\ \text{---} \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{c}_R \\ \text{---} \end{bmatrix} = \begin{bmatrix} | & & | \\ \mathbf{A} & & \\ | & & | \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{D} \\ \text{---} \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{C} \\ \text{---} \end{bmatrix} \begin{bmatrix} \text{---} \\ \mathbf{B}^T \\ \text{---} \end{bmatrix}$$

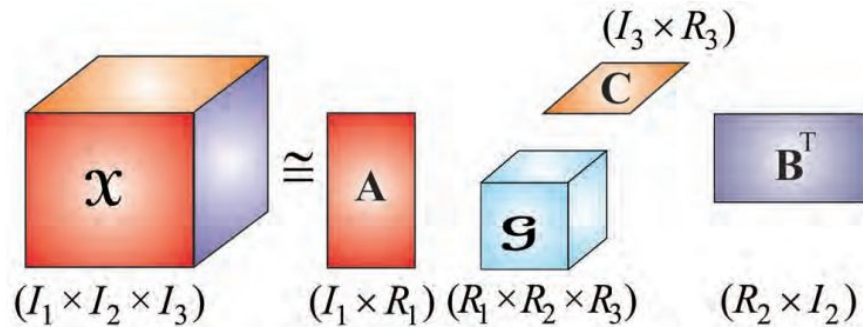
$(I \times R)$ $(R \times R \times R)$ $(K \times R)$ $(R \times J)$

Kruskal vs Tucker Tensor Decomposition

Kruskal Decomposition:



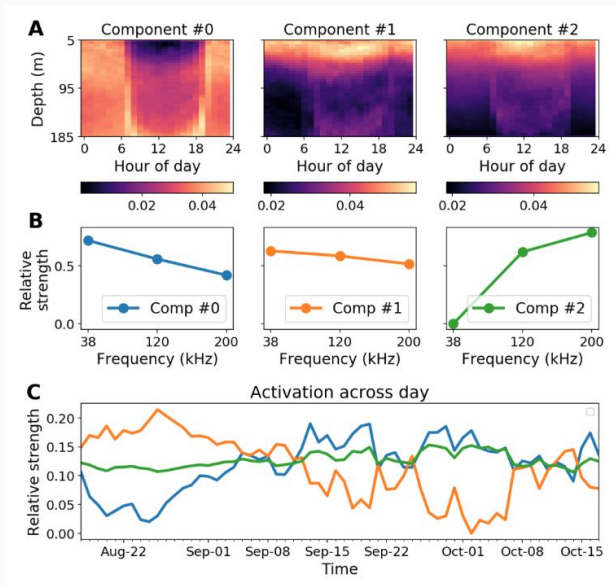
Tucker Decomposition:



Tensor Decomposition Results

Kruskal Nonnegative Tensor Decomposition

[tensorly](#) package



Automate heuristic methods based on thresholding rules about the frequency response which depend on correct calibration.

Tensor Decomposition Considerations

The rank-1 constraint of the Kruskal Decomposition is very limiting:

- Maximum 3 components (the lowest dimension)
- Components should have the same frequency response
- More noise in the reconstruction

The solution is almost certainly unique (as opposed to matrix decomposition)

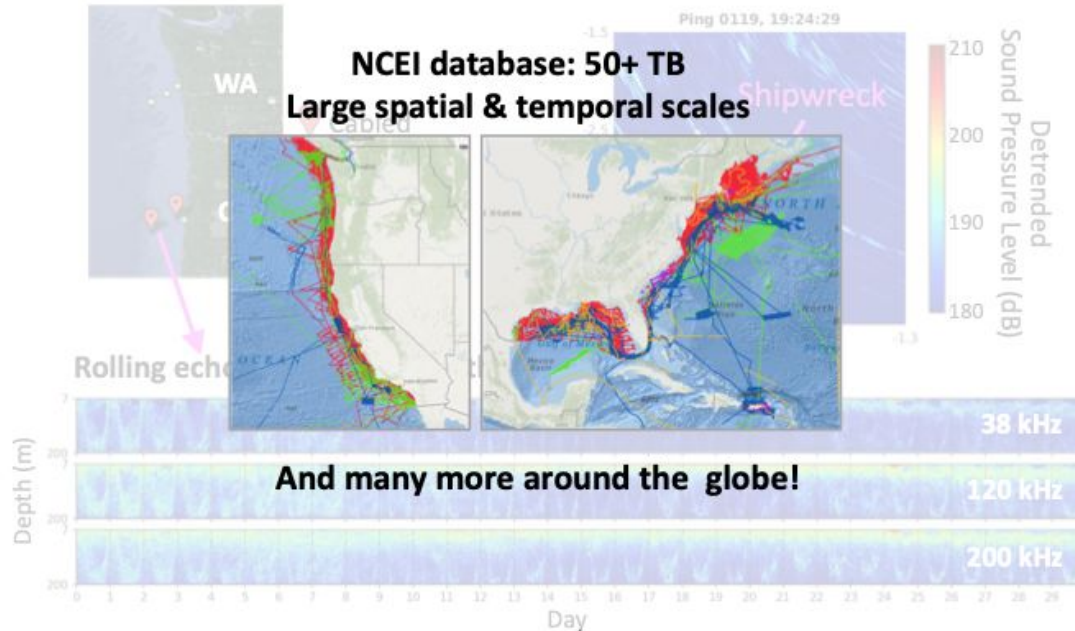
Better suited for broadband data: many frequencies

Future: Many Large Datasets to Analyze

Examples of large scale sonar data

Large temporal scale
OOI Endurance array

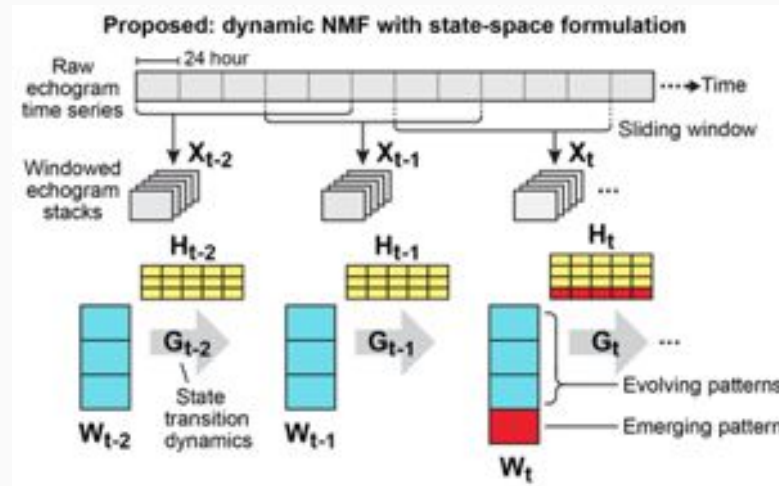
Large spatial scale
Dusk migration of reef fish



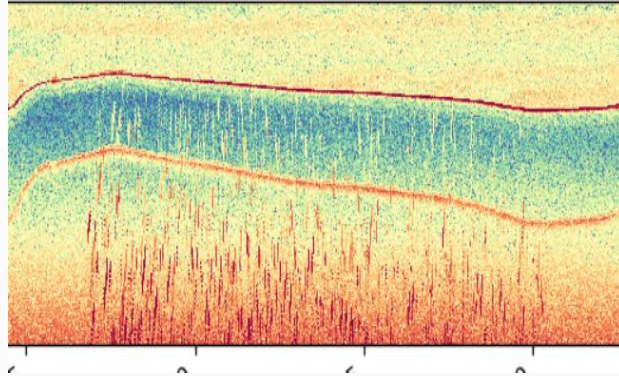
Future: Emerging, Evolving, and Fading Patterns

Within long time series the patterns are gradually changing over time:

- Add constraints on the patterns W (as opposed to the activations).



Future: Application to Ship Data

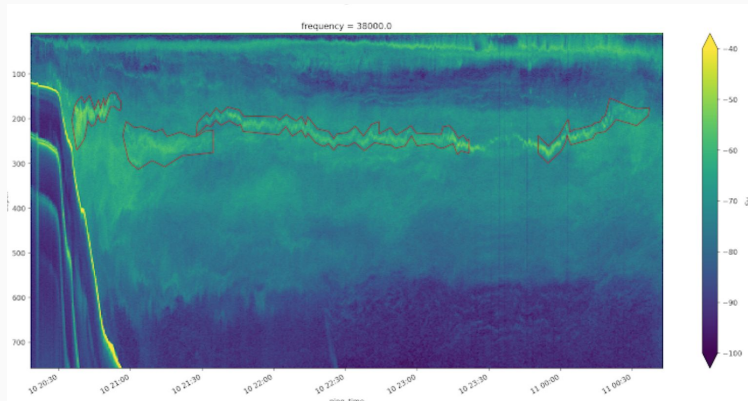


Ship is moving!

- Bottom variation
- Environment variation
- Ship speed variation

Future: Compare to Ground Truth

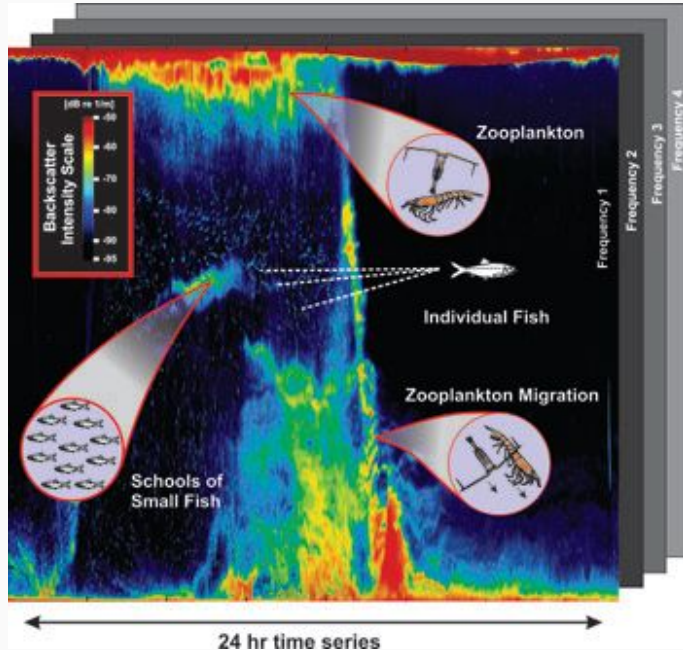
- Survey Cruise annotations
- Trawl data



Collaborating with NOAA Northwest Fisheries Science Center

Water Column Sonar Data

Data: depth, time, frequency



Goals:

- Discover patterns of marine organism activities
 - Distinguish between fish and zooplankton
 - Estimate species abundance
 - Detect migrational patterns
- Relate to physical processes and external phenomena